

# Impact of Optical Modes on the Pairing Potential in Bilayer Cuprates

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Superconducting transition temperature is calculated for differently doped bilayer cuprates. Superexchange is assumed to be the dominating mechanism of high-temperature superconductivity, but the contribution from the phonon potential is not negligible, which qualitatively explains the observed weak isotopic effect. The calculated value  $2\Delta_{max}/k_B T_C \simeq 4.5$  is close to the experiment in the case of optimum doping.

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Journal ref:

Izvestiya Rossijskoj Akademii Nauk, Physics Series, Vol. **62**, No. 8, pp. 1518-1521 (1998).

Corrected English translation: Bulletin of the Russian Academy of Sciences: Physics, Vol. **62**, No. 8, pp. 1228-1230 (1998).

PACS numbers: 74.20.Fg, 74.60.Mj, 74.70.Jm

## I. INTRODUCTION

The High Temperature Superconductivity (HTSC) was discovered 11 years ago. None of the proposed HTSC mechanisms has been commonly accepted yet (see [1]). Unlike the case in normal low-temperature superconductors, the energy gap in HTSC materials is different at different points of the Brillouin zone. This dependence is important, for the understanding of the HTSC mechanism.

In [2,3] we found solutions of the Bardeen-Cooper-Schrieffer (BCS) equations taking copper spin superexchange into consideration. This interaction was found to lead to a reasonable critical temperature  $T_C$  and  $d$ -symmetry of the energy gap in superconducting cuprates. The conclusion about the  $d$ -symmetry of the order parameter was confirmed by recent studies of photoemission spectra [4]. In the present work we additionally consider the electron - phonon interaction with optical buckling  $A_{1g}$ ,  $B_{1g}$  and breathing  $A_g$ ,  $E_g$  modes to explain the weak isotope effect in these compounds.

## II. POTENTIAL OF CURRENT CARRIERS PAIRING THROUGH OPTICAL BUCKLING AND BREATHING MODES

In the compound  $\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$  holes interact most strongly with an electric field perpendicular to the  $\text{CuO}_2$  plane. This field is mainly induced by triply charged yttrium ions [5]. The operator of binding energy with oscillations perpendicular to the  $\text{CuO}_2$  plane has the form

$$H_{h-ph} = e \sum_{n\sigma} \left\{ \mathbf{E}_x \mathbf{u}_x \left( a\mathbf{n} + \frac{a\mathbf{x}}{2} \right) p_{nx}^{\sigma\sigma} + \mathbf{E}_y \mathbf{u}_y \left( a\mathbf{n} + \frac{a\mathbf{y}}{2} \right) p_{ny}^{\sigma\sigma} \right\}, \quad (1)$$

where  $p_{nx}^{\sigma\sigma}$  and  $p_{ny}^{\sigma\sigma}$  are the Hubbard operators of oxygen holes,  $\mathbf{u}_x(n)$  and  $\mathbf{u}_y(n)$  are the displacements vectors of O(2) and O(3) positions in a unit cell with the number  $n$ ,  $\mathbf{x}$  and  $\mathbf{y}$  are unit vectors of the axes  $a$  and  $b$  respectively,  $a$  is the lattice constant, and  $E_x = 1.2 \cdot 10^8 \text{ V}\cdot\text{cm}^{-1}$ ,  $E_y = 1.5 \cdot 10^8 \text{ V}\cdot\text{cm}^{-1}$  are the components of electric field along the the axis  $c$ , calculated in [6]. For simplicity, we put  $E = E_x = E_y = 1.35 \cdot 10^8 \text{ V}\cdot\text{cm}^{-1}$ . Then, calculating the commutator  $[\Psi_{\mathbf{k}}^{\downarrow, pd}, H_{h-ph}]$  and using the expression

$$\left[\Psi_{\mathbf{k}}^{\downarrow,pd}, H_{h-ph}\right] = \sum_{\alpha, \mathbf{q}} V^{\alpha}(\mathbf{q}) \Psi_{\mathbf{k}-\mathbf{q}}^{\downarrow,pd} (b_{\mathbf{q}} + b_{-\mathbf{q}}^{\dagger}),$$

where  $\Psi_{\mathbf{k}}^{\downarrow,pd}$  is the quasiparticle operator of singlet-correlated oxygen holes,  $b_{-\mathbf{q}}^{\dagger}$  and  $(b_{\mathbf{q}})$  are the phonon creation and annihilation operators, one finds

$$V^{\alpha}(\mathbf{q}) = \frac{e}{2} E \sqrt{\frac{\hbar}{2m\omega_{\alpha}}} \left[ \cos\left(\frac{q_x a}{2}\right) \pm \cos\left(\frac{q_y a}{2}\right) \right], \quad (2)$$

where  $\omega_{\alpha} = \omega_{A_{1g}} = 440 \text{ cm}^{-1}$  and  $\omega_{B_{1g}} = 340 \text{ cm}^{-1}$  [7]. The plus and minus signs correspond to the modes  $A_{1g}$  and  $B_{1g}$  respectively,  $e$  is the electron charge, and  $m$  is the mass of the unit cell. Since the difference between  $\omega_{A_{1g}}$  and  $\omega_{B_{1g}}$  is not so important, they are put equal to  $\omega_G = 400 \text{ cm}^{-1}$ .

Using the Frohlich procedure, the potential of current carriers interacting through the phonon field of buckling modes  $A_{1g}$  and  $B_{1g}$  is written as

$$G(\mathbf{k}' - \mathbf{k}) = 2G_0^2 \frac{1 + \frac{1}{2} [\cos(k'_x - k_x) a + \cos(k'_y - k_y) a]}{(\varepsilon_{\mathbf{k}'} - \varepsilon_{\mathbf{k}})^2 - (\hbar\omega_G)^2} \hbar\omega_G, \quad (3)$$

where  $G_0 = 35 \text{ meV}$ .

Assuming that the constant of interaction with the modes  $A_g$  and  $E_g$  (and their frequencies) are identical, the contribution to the pairing potential is written as

$$B(\mathbf{k}' - \mathbf{k}) = 2B_0^2 \frac{1 - \frac{1}{2} [\cos(k'_x - k_x) a + \cos(k'_y - k_y) a]}{(\varepsilon_{\mathbf{k}'} - \varepsilon_{\mathbf{k}})^2 - (\hbar\omega_B)^2} \hbar\omega_B. \quad (4)$$

According to the estimate of [8], the constant  $B_0$  is about 60 meV. The frequencies  $\omega_{A_g}$  and  $\omega_{E_g}$ , taken from [9], are about  $480 \text{ cm}^{-1}$ .

### III. EQUATION FOR THE GAP

The BCS equation for the energy gap, taking into account the interaction via the phonon field and the superexchange between copper spins, has the form

$$\Delta_{\mathbf{k}'} = \sum_{\mathbf{k}} \left\{ P^2 [G(\mathbf{k}' - \mathbf{k}) + B(\mathbf{k}' - \mathbf{k})] \theta(\hbar\omega_D - |\varepsilon_{\mathbf{k}'} - \varepsilon_{\mathbf{k}}|) - J^{dd}(\mathbf{k}' - \mathbf{k}) \right\} \langle \Psi_{\mathbf{k}}^{\downarrow,pd} \Psi_{-\mathbf{k}}^{\uparrow,pd} \rangle, \quad (5)$$

where  $J^{dd}(\mathbf{q})$  is the Fourier transform of the superexchange parameter  $J = 57 \text{ meV}$ ,

$$J^{dd}(\mathbf{q}) = 2J (\cos q_x a + \cos q_y a),$$

$\omega_D = 500 \text{ cm}^{-1}$  is the Debye frequency, and  $P = \frac{1}{2}(1+x)$ . The correlation function is given by

$$\langle \Psi_{\mathbf{k}}^{\downarrow,pd} \Psi_{-\mathbf{k}}^{\uparrow,pd} \rangle = -\frac{\Delta_{\mathbf{k}}}{2E_{\mathbf{k}}} \tanh\left(\frac{E_{\mathbf{k}}}{2k_B T}\right),$$

where  $E_{\mathbf{k}} = \sqrt{(\varepsilon_{\mathbf{k}} - \mu)^2 + \Delta_{\mathbf{k}}^2}$ . The chemical potential  $\mu$  and the hole concentration  $x$  for two copper sites in the bilayer (assuming that the antibonding band is empty) are related as

$$x = P \sum_{\mathbf{k}} \left[ \exp\left(\frac{\varepsilon_{\mathbf{k}} - \mu}{k_B T}\right) + 1 \right]^{-1}.$$

At  $x = 0.33$  the chemical potential is placed on 10 meV below the saddle singularity peak in the density of states. The dispersion  $\varepsilon_{\mathbf{k}}$  is chosen as

$$\varepsilon_{\mathbf{k}} = P [2t_1 (\cos k_x a + \cos k_y a) + 4t_2 \cos k_x a \cos k_y a + 2t_3 (\cos 2k_x a + \cos 2k_y a)], \quad (6)$$

where  $t_1$ ,  $t_2$ , and  $t_3$  are the effective hopping integrals. All the calculations are carried out at  $t_1 = 70 \text{ meV}$ ,  $t_2 = 0$ , and  $t_3 = 5 \text{ meV}$ .

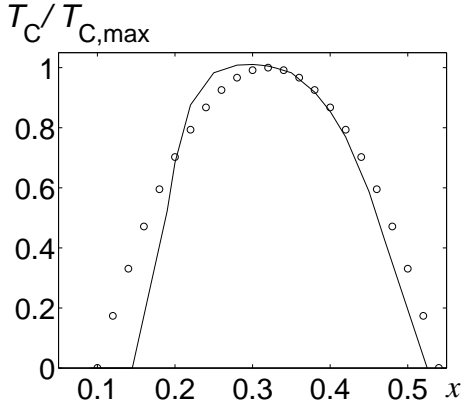


FIG. 1. Temperature dependence of the superconducting transition temperature in  $\text{YBa}_2\text{Cu}_3\text{O}_{7-y}$  with doping: solid line (calculations) and the experimental points are sketched by open circles.

Figure 1 shows the dependence of the superconducting transition temperature of  $\text{YBa}_2\text{Cu}_3\text{O}_{7-y}$  with doping. It is evident that the calculations qualitatively conform with the experimental data (normalized by the expression  $T_C/T_{C,max} = 1 - 82.6(x - 0.32)^2$  [10]). However, their noncoincidence remains unexplained. Numerical solution of the energy gap equation yields a  $d$ -type symmetry of the order parameter  $\Delta_{\mathbf{k}} = \Delta_0(\cos k_x a - \cos k_y a)$  and a nonstandard value of  $2\Delta_{max}/k_B T_C \approx 4.5$  with the superconducting transition temperature  $T_{C,max} \sim 100$  K. Note that solutions of (5) with  $J = 0$  lead to the  $s$ -type symmetry of the gap,  $\Delta_{\mathbf{k}} = \Delta_0(\cos k_x a + \cos k_y a)$ . The conclusion of [11] that the  $d$ -symmetry of the gap arises from pairing only through optical buckling modes seems to be groundless.

#### IV. CONCLUSION

Self-consistent solutions of the BCS gap equation are found in the class of short-range pairing potentials for various chemical potentials. When the Fermi level  $\varepsilon_F$  is near the bottom(top) of the band, the solutions correspond to the  $s$ -type pairing, while for  $\varepsilon_F$  in the center of the band the solution are related to the  $d$ -type. The short-range potentials considered are (i) superexchange interaction, (ii) interaction of current carriers via optical oscillations, and (iii) breathing and buckling modes of oxygen atoms in  $\text{CuO}_2$  planes. The superconducting transition temperature is calculated for various oxygen indices  $x$ .

The dominant HTSC mechanism is a superexchange. However, the contribution of the phonon pairing is not negligible, that qualitatively explains the observed weak isotope effect. The calculated value  $2\Delta_{max}/k_B T_C \approx 4.5$  is close to the experiment.

The work was partially supported by the Federal Program "Superconductivity" (Grant 94029) and the Russian Foundation for Basic Research under Project Code 97-02-16235.

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